

How to Fit the Data to a Least Squares Regression Line

Without getting into too much technical detail, the least squares regression line is the straight line that "best fits" the data. The metric for determining best fit is to measure the square of the distance from each point to the best fit line, sum those squares, and then select the line that minimizes that sum. Fortunately, this has been studied and converted to formulas.

The best fit line is expressed in the form $y = B_1x + B_0$, where formulas exist for determining B_1 and B_0 .

$$B_1 = \frac{SS_{xy}}{SS_{xx}} \quad \text{where} \quad SS_{xy} = \sum xy - (1/n)(\sum x)(\sum y) \quad \text{and} \quad SS_{xx} = \sum x^2 - (1/n)(\sum x)^2$$

The summation sign Σ refers to summing up each value of x or y , as appropriate. In our case we have $n = 3$ points with (x,y) values $(2, 469)$, $(3, 615)$, and $(4, 1,058)$. The math is shown below:

$$\begin{aligned} SS_{xy} &= (2)(469) + (3)(615) + (4)(1058) - (1/3)(2 + 3 + 4)(469 + 615 + 1,058) = \\ &= 938 + 1,845 + 4,232 - (1/3)(9)(2,142) = 7,015 - 6,426 = 589 \end{aligned}$$

$$SS_{xx} = 2^2 + 3^2 + 4^2 - (1/3)(2 + 3 + 4)^2 = 4 + 9 + 16 - (1/3)(9^2) = 29 - 27 = 2$$

$$\text{Thus } B_1 = 589 / 2 = 294.5$$

The formula for B_0 is: $B_0 = (1/n)(\sum y) - B_1(1/n)(\sum x)$

$$\begin{aligned} \text{Thus } B_0 &= (1/3)(469 + 615 + 1,058) - (294.5)(1/3)(2 + 3 + 4) = \\ &= 714 - (294.5)(3) = -169.5 \end{aligned}$$

Thus the least squares regression line is: $y = 294.5x - 169.5$

The B_1 and B_0 parameters can also be determined in Excel using the SLOPE and INTERCEPT functions. In each case the functions are applied to a data range of y values, followed by a comma and the data range of x values.

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